

An Improved Space Charge Limited Emission Algorithm in VSim

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Available in VSim II!



SIMULATIONS EMPOWERING INNOVATION



For more details on this work, see the recent publication in Phys Plasmas

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A new simple algorithm for space charge limited emission

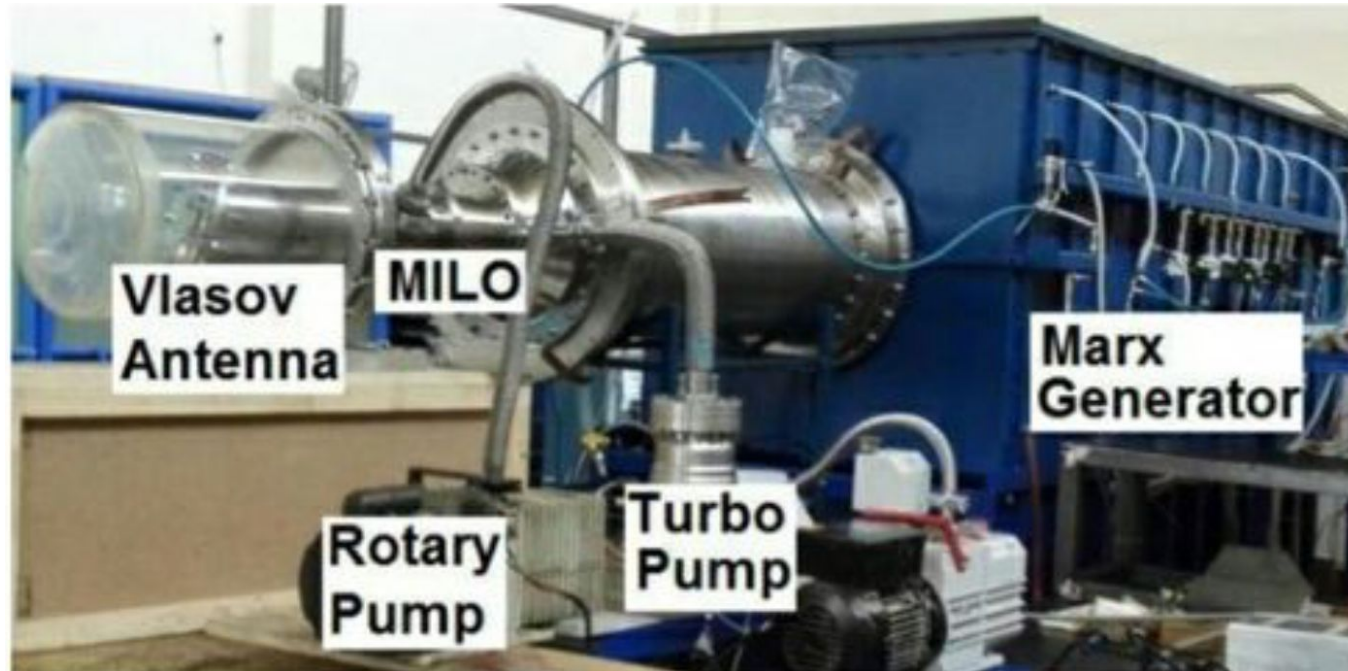
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Many devices in the directed energy community seek to operate at the highest possible power

MILO -
Magnetically
Insulated Line
Oscillator

A MILO
converts DC
input to rf
output using a
high current
electron beam

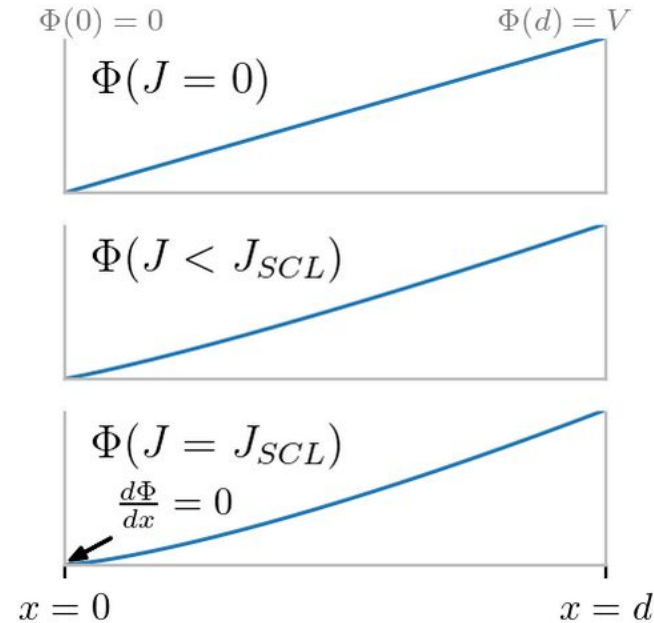
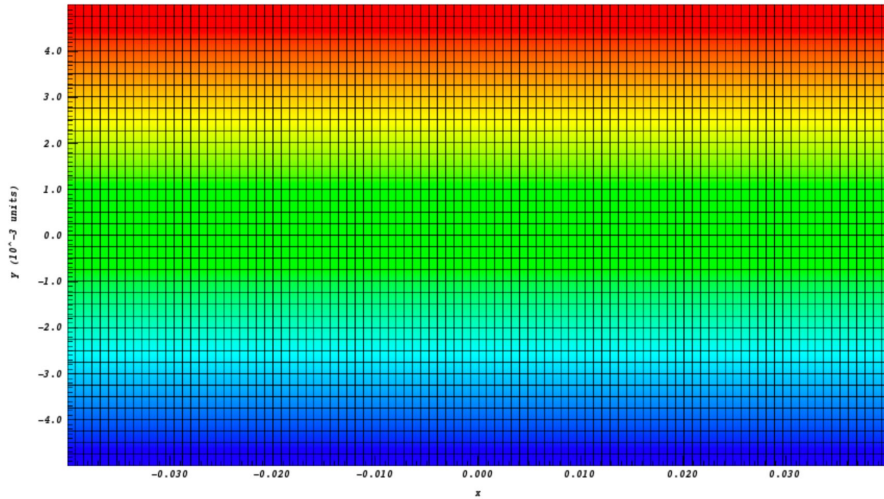


Researchers often
want microwaves
devices (like the
MILO shown here)
to operate at the
highest possible
power...and
current!

But simulating ultra-high current can be challenging!

But let's start simple...just electron flow between two parallel plates

Potential between two plates in VSim



$$J_{SCL} = \frac{4}{9} \epsilon_0 \sqrt{\frac{2e}{m}} \frac{V^{\frac{3}{2}}}{d^2}$$

SCL = Space Charge Limit
CL = Child-Langmuir
(in 1D, steady state, they are the same)

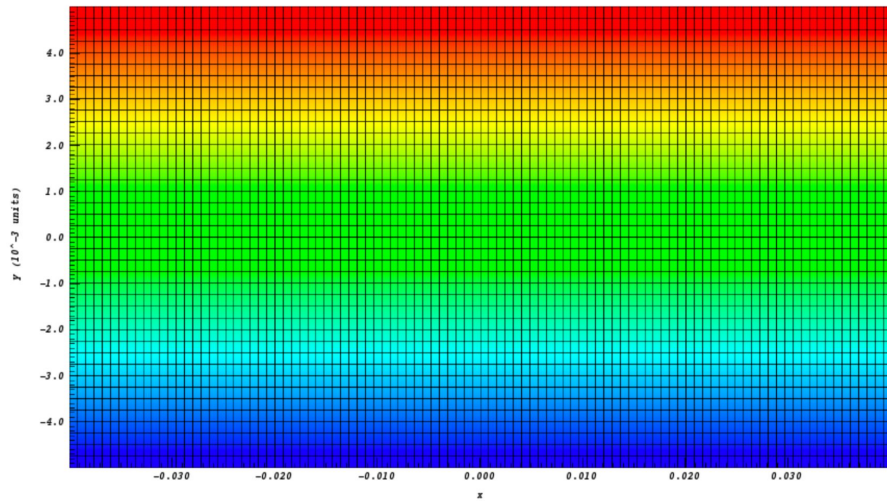
The 1D case is described by a theoretical expression, the Child-Langmuir equation

Short interlude: the fascinating career of Katherine Blodgett



- First woman to get a PhD in physics from Cambridge
- First woman physicist hired by GE Research
- Generalized the 1D planar Child-Langmuir equation to cylindrical and spherical geometries (along with Langmuir)
- You will hear often of the Langmuir-Blodgett equation instead of the Child-Langmuir equation in complex geometries!

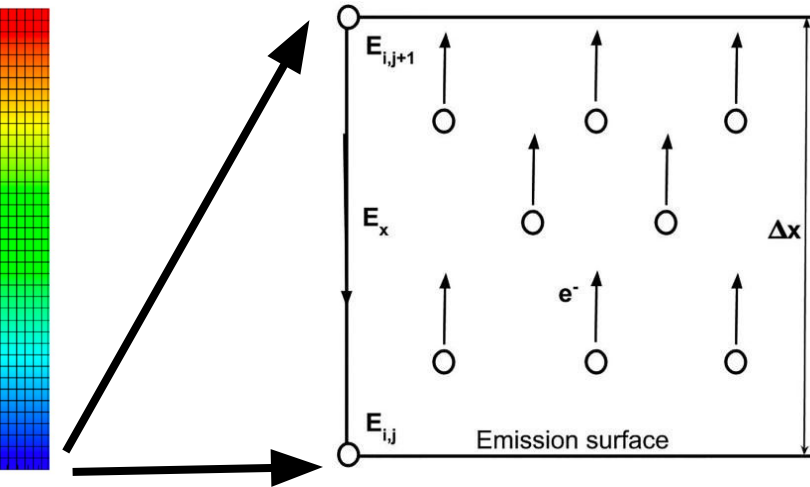
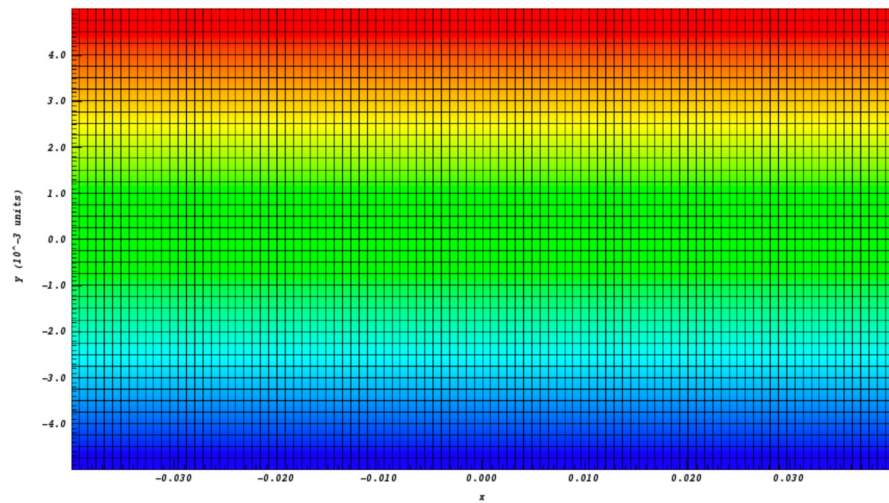
My speciality: what's the wrong way to solve this problem?



$$J_{\text{SCL}} = \frac{4}{9} \epsilon_0 \sqrt{\frac{2e}{m}} \frac{V^{\frac{3}{2}}}{d^2}$$

- *First time step:* This problem is so easy! You know V and d . Just plug them in and emit that much current!
- *Second time step:* V and d didn't change... Oh...shoot...wait...there's already some current in my system!
- So OK...now calculate the current you already have and just emit however much current you need to get to J_{SCL} ?
- *Third time step:* Oh boy! Now some current is actually going the wrong way. Do I include that? No? Yes?
- V and d still haven't changed! I keep having to emit the same current even though there's already current present.

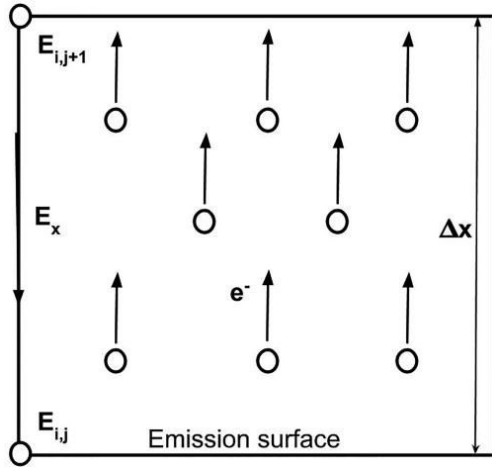
Better way: take advantage of the FDTD grid to make a natural SCL emission scheme!



Blow-up image of the first zone

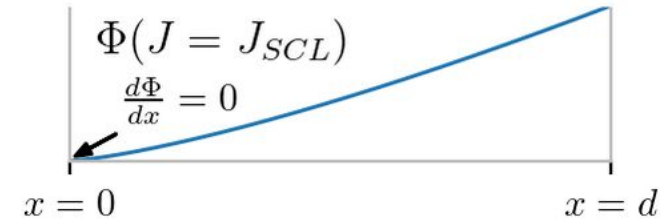
$$J_{\text{emit}} = \frac{4}{9} \epsilon_0 \sqrt{\frac{2e}{m}} \frac{E_0^{\frac{3}{2}}}{\sqrt{\Delta x}}$$

But is it strange for the current to depend on the cell size?



$$J_{\text{emit}} = \frac{4}{9} \epsilon_0 \sqrt{\frac{2e}{m}} \frac{E_0^{\frac{3}{2}}}{\sqrt{\Delta x}}$$

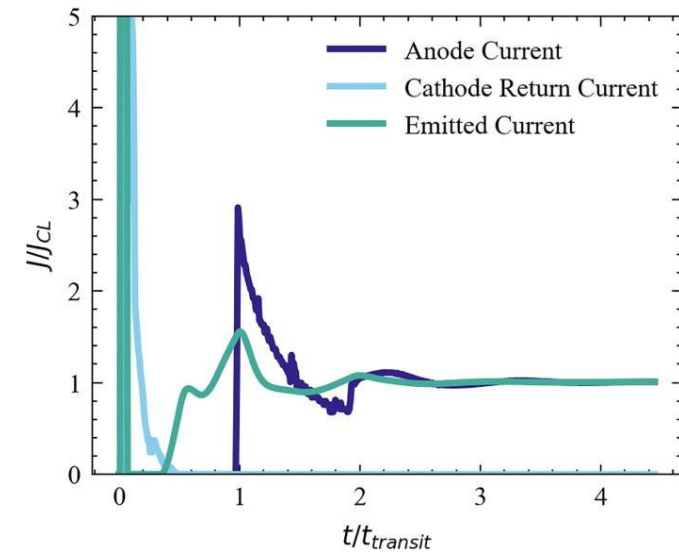
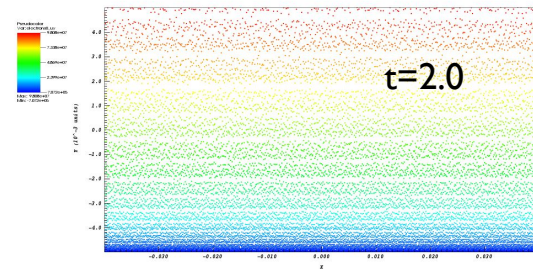
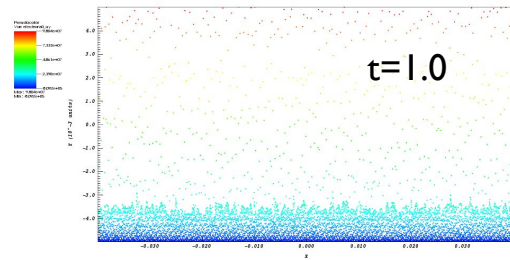
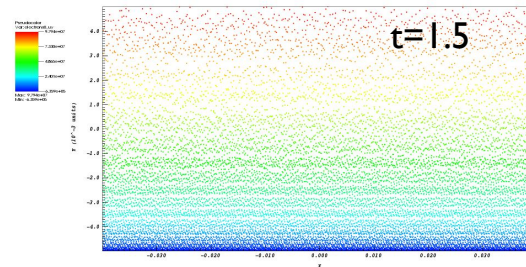
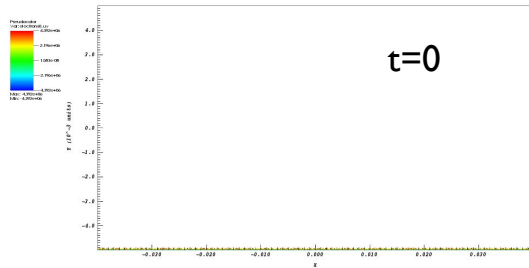
Doesn't that mean
better resolution
will lead to
diverging current?



No! Because E is
going to zero at the
surface, and the two
effects cancel out.

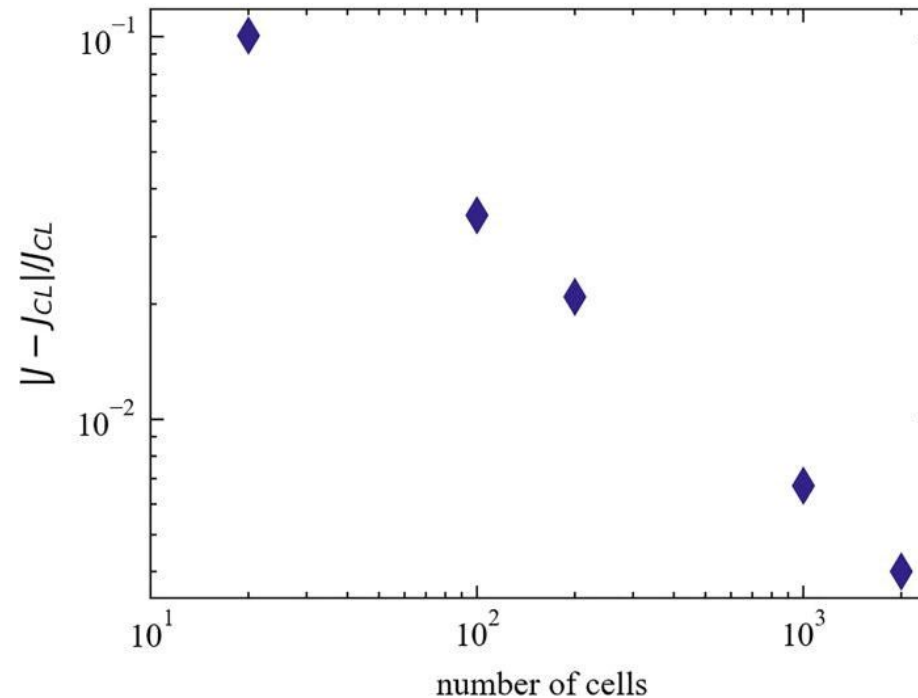
The current is
constant with
changing resolution!

The ID diode test shows the new algorithm works well!



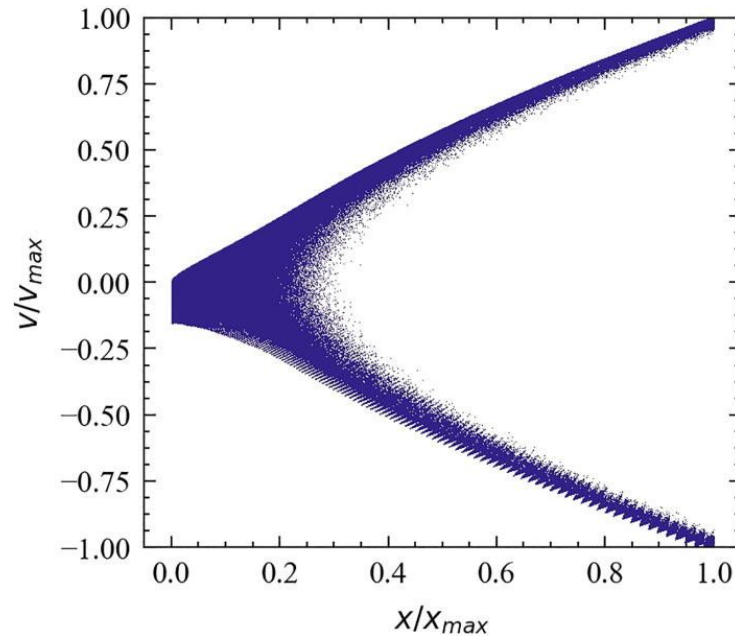
The ID diode reaches a steady state in just a few transit times

As we improve the resolution, we get closer to the analytic answer

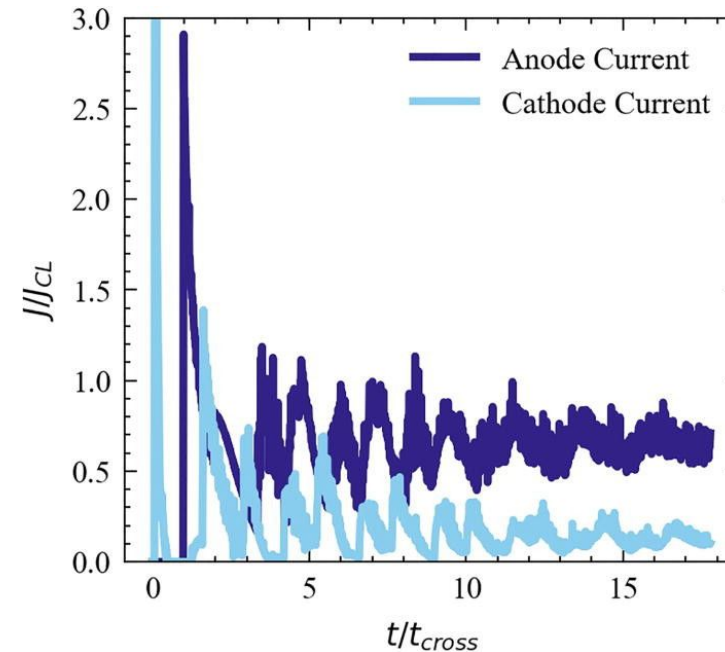


The error converges like the number of cells to the $-2/3$ power, consistent with the fact the theoretical electron density scales as $2/3$ power.

The algorithm is robust enough to handle even more complicated cases, like secondary electron emission

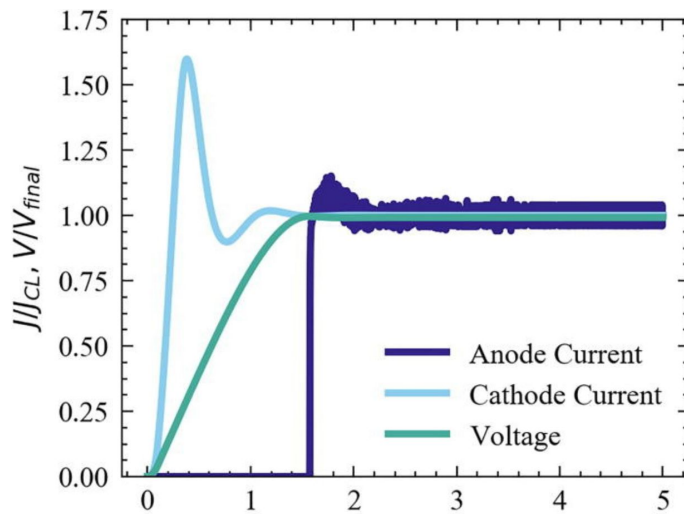


The electron phase space for the case where the anode is a perfect elastic electron reflector.

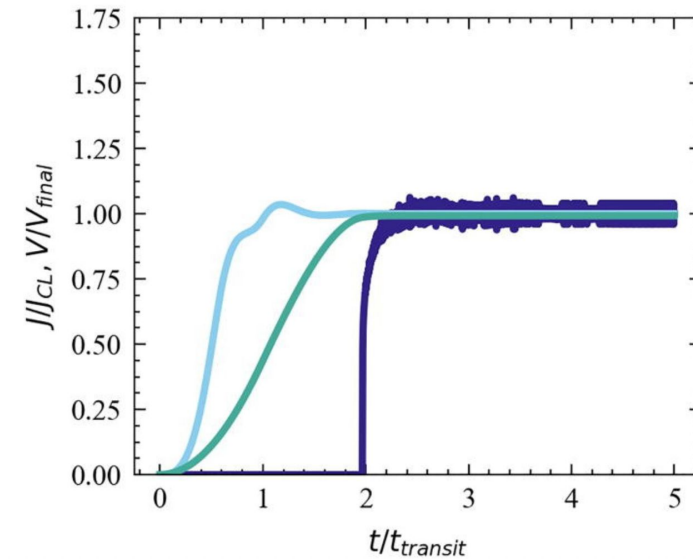


The current density at the anode and re-absorbed at the cathode. The simple estimate of steady-state current at the anode of $0.5 J_{CL}$ is a slight under-estimate due to virtual cathode formation.

The algorithm also captures accurately time-dependent voltage effects

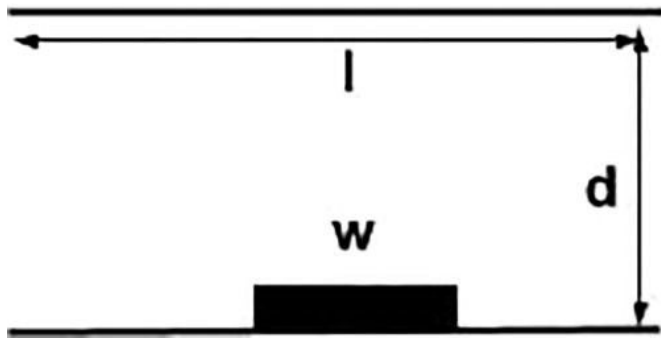


A fast voltage rise can cause inductive spikes, and our algorithm captures that

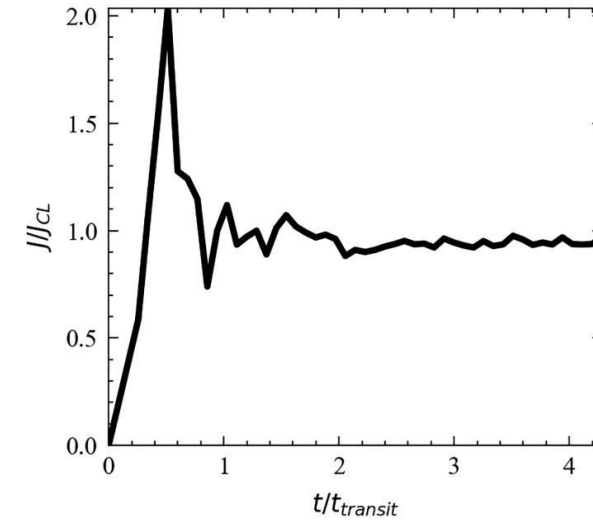


A slower voltage rise can moderate those inductive spikes

What about 2d? For instance, if the emission region has finite size

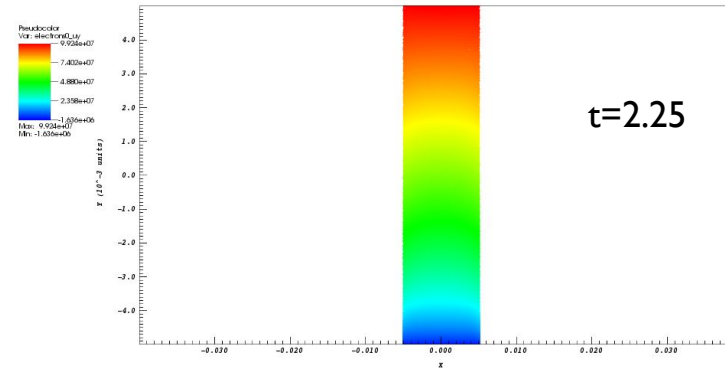
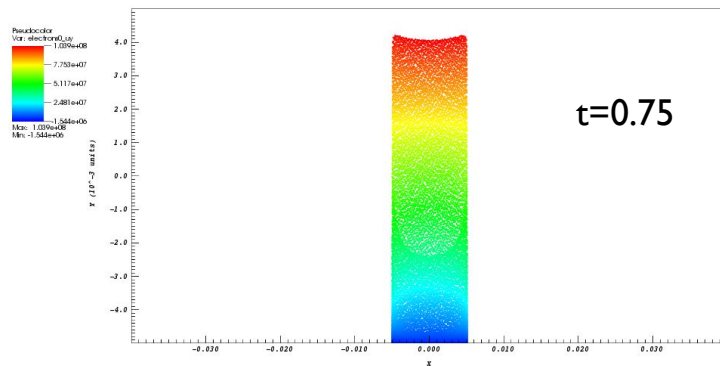
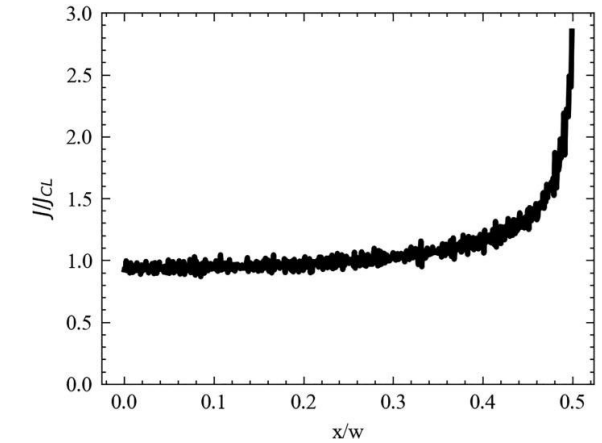
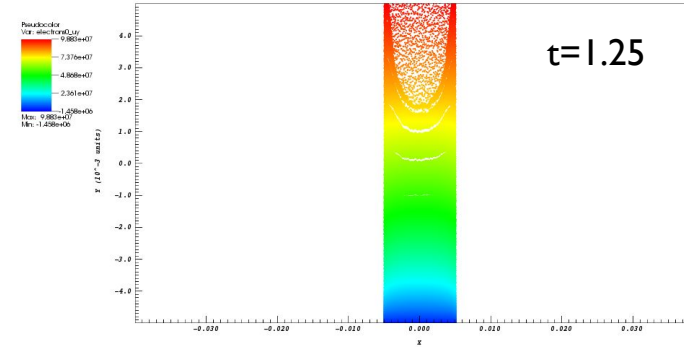
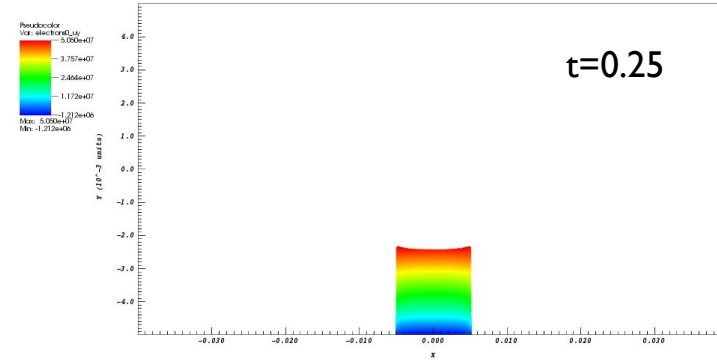


No analytic answer, but there are well-known numerical answers to which we can compare.



The current right in the center of the anode shows the same behavior as 1D.

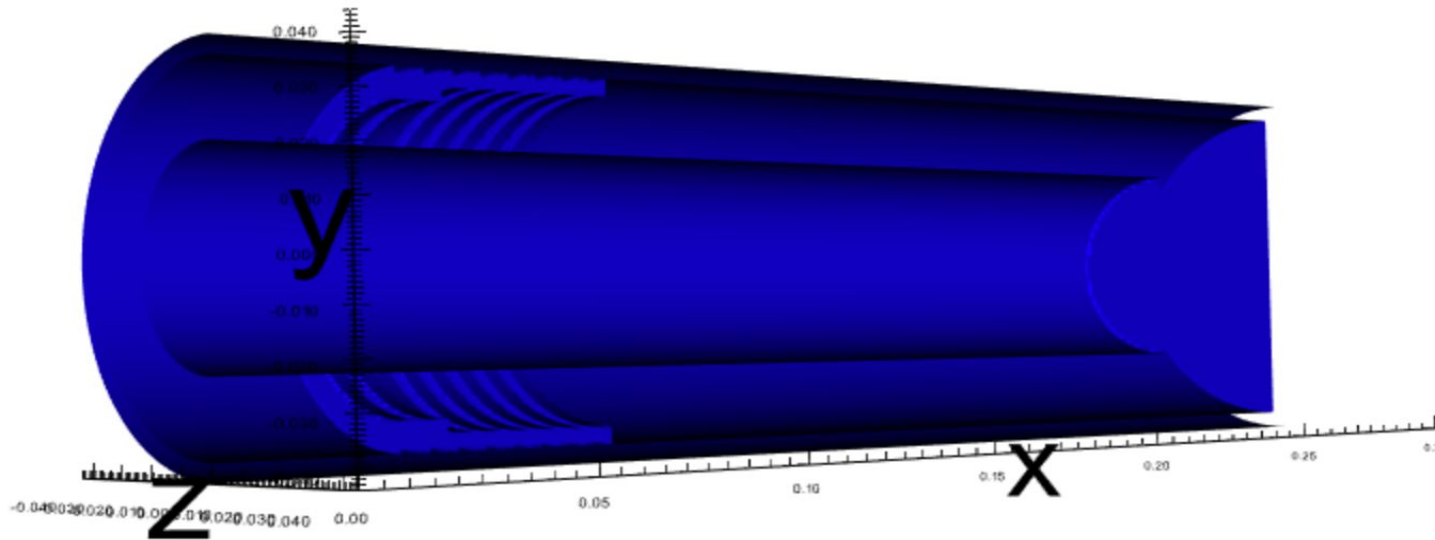
The VSim results show a factor of three enhancement that matches previous well-known numerical results*



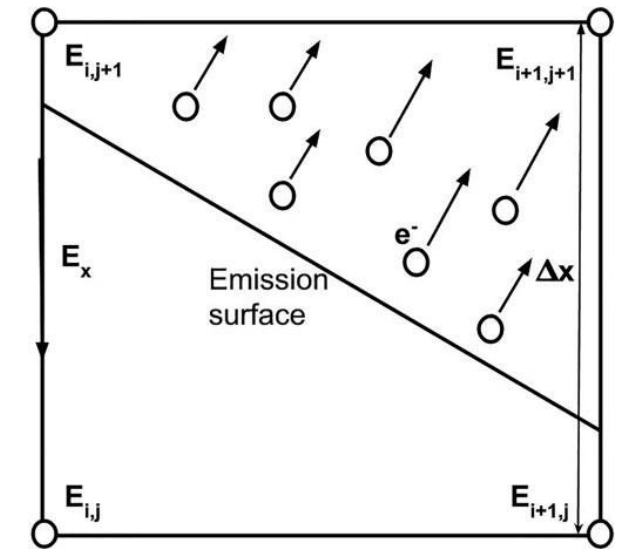
The current density as a function of space after several transit times.

*J. J. Watrous, J. W. Lugisland, and G. E. Sasser, "An improved space-charge-limited emission algorithm for use in particle-in-cell codes," Physics of Plasmas 8, 289–296 (2001)

With benchmarking done, we are ready to apply this new algorithm to a MILO

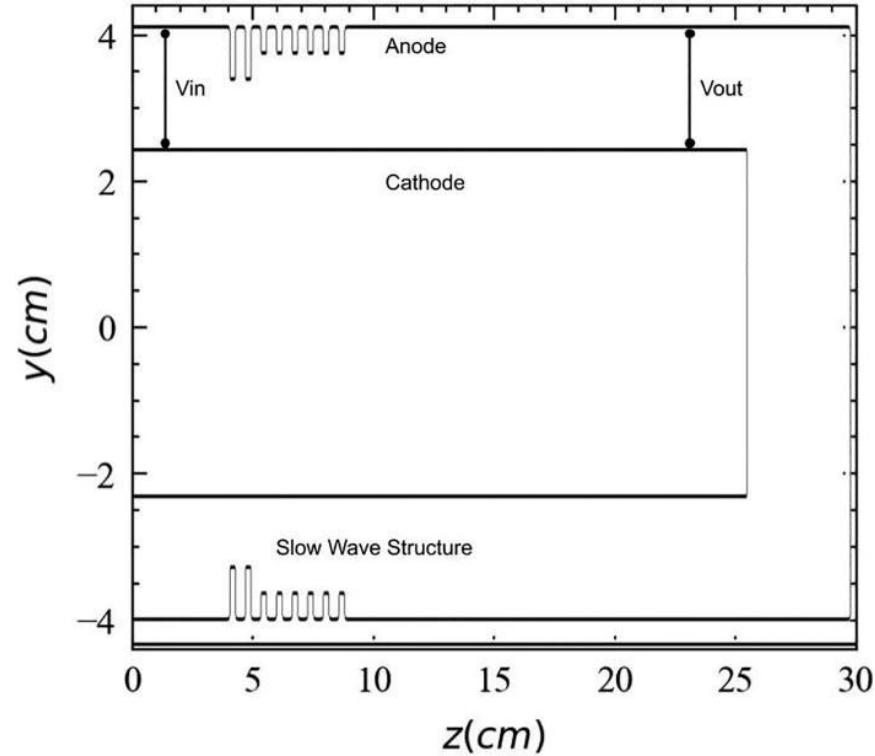


We model the MILO in full 3D with the geometry handled through the VSim embedded boundary capabilities.



The VSim SCL emission algorithm leverages this capability to work even in complex geometries

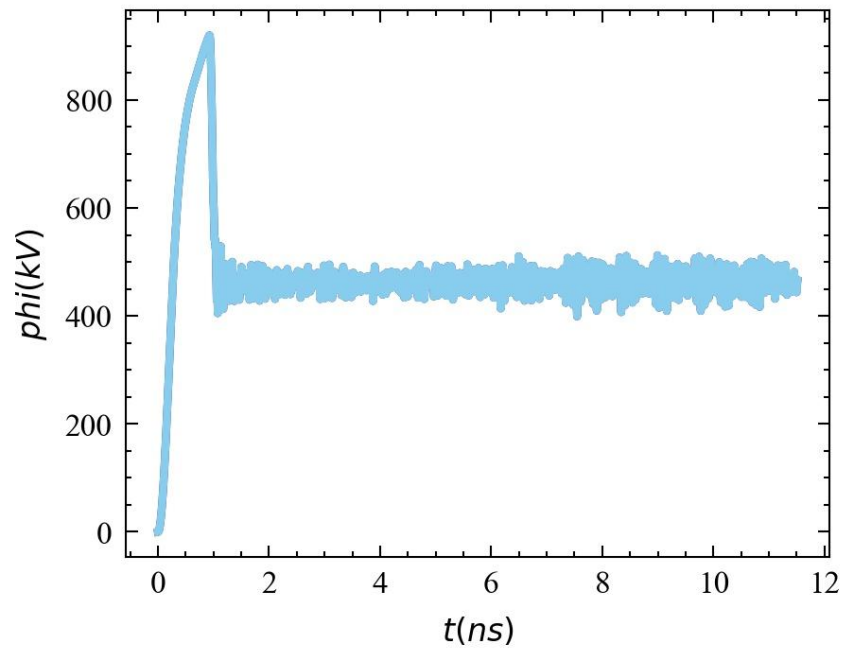
A MILO converts DC to rf using the interaction of the electron beam with a rippled structure on the anode



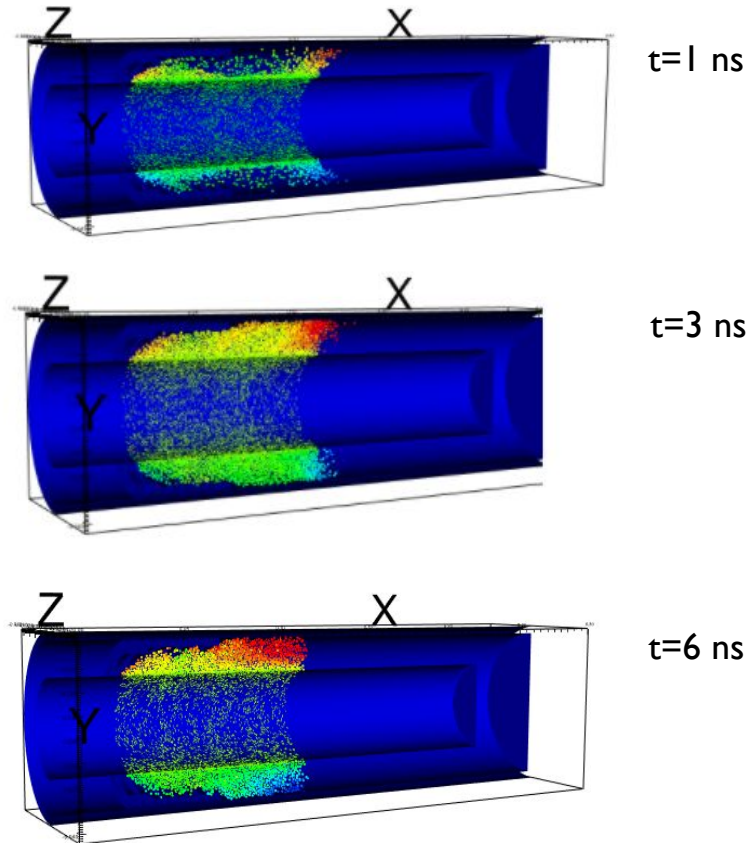
We will drive V_{in} with a 500kV DC voltage, let the cathode emit electrons at the SCL value, and observe the output voltage

We apply the new SCL emitter to the MILO

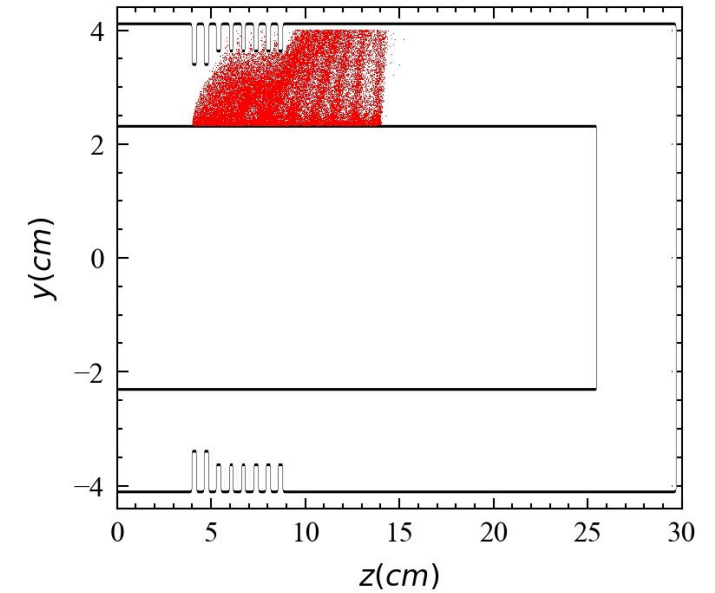
Applied Voltage



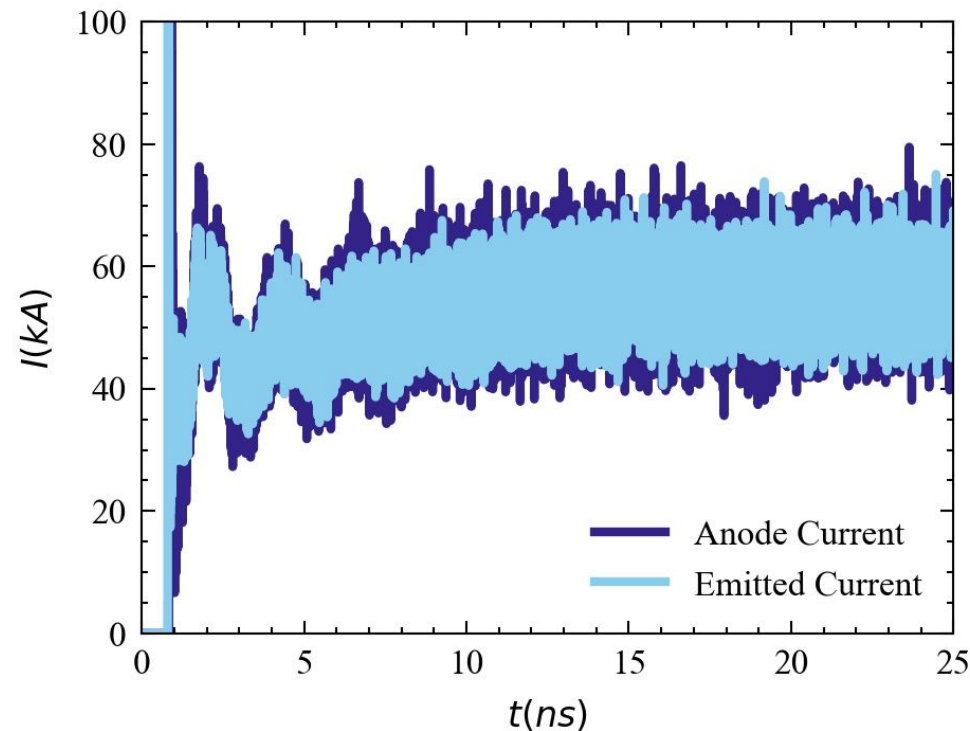
Resulting SCL particles
(colored by velocity)



Spoke formation is the
sign of rf power!

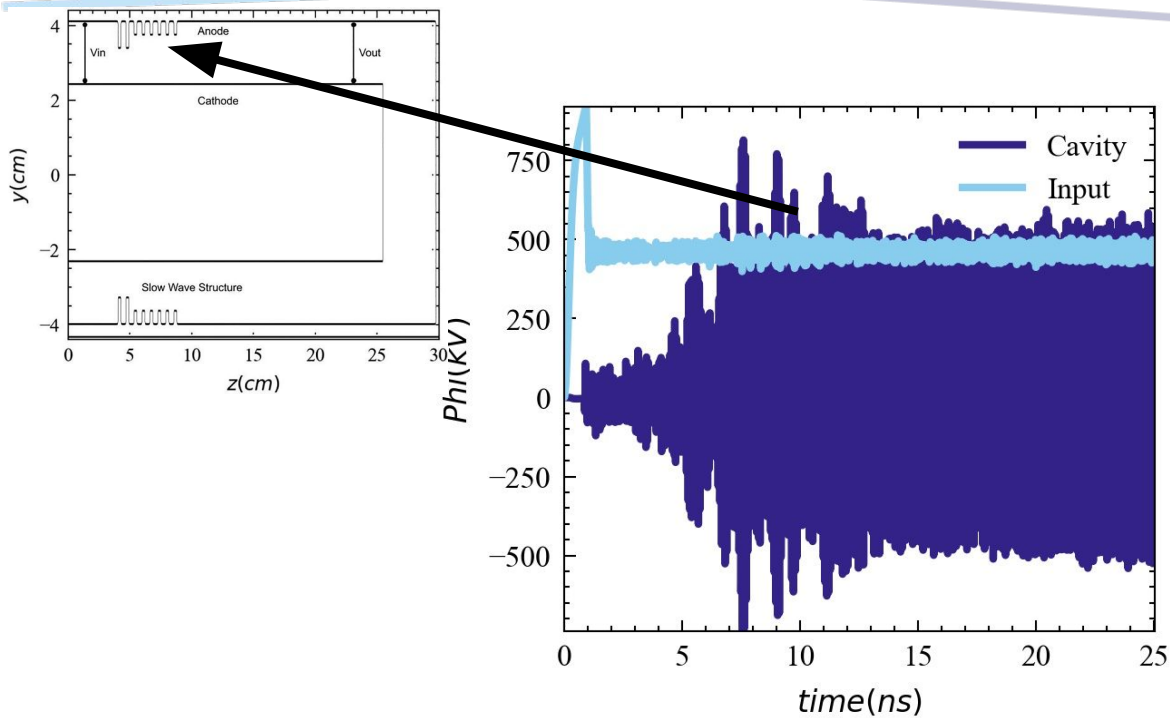


The emitted and absorbed current of 50kA, in line with a 500kV device of this size

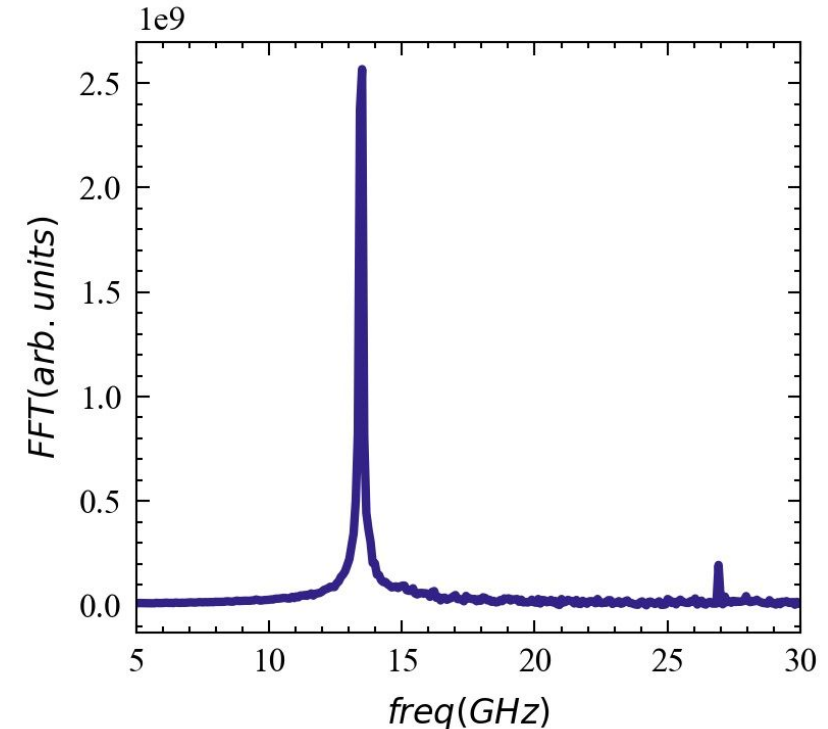


Agrees with
Langmuir-Blodgett
(when adjusted for
relativistic effects)

The frequency of the rf is 13 GHz, matching previous results*



The input DC voltage of 500kV is converted to rf voltage in the anode cavities



The main frequency is 13 GHz, matching previous results. The presence of harmonics is another indication the SCL algorithm is working well.

*T. Jiang, J. Zhang, J. He, Z. Li, and J. Ling, "Experimental research on ku-band magnetically insulated transmission line oscillator," Physics of Plasmas 22, 102112 (2015)

Thanks for your attention!

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